

Factor each of the following.

$$
\begin{array}{rlrl}
\text { a) } x^{2}-11 x+28 & & \text { b) } 12 x^{2}-5 x-2 \\
=(x-4)(x-7) M 28 & =12 x^{2}+3 x-8 x-2 \\
A-11 & =3 x(4 x+1)-2(4 x+1) \\
M-4,-7 & =(4 x+1)(3 x-2)
\end{array}
$$


$\begin{array}{ccc}M & -24 & 24 \\ A & -5 & 1,24 \\ N & -8,3 & 2,12 \\ 3,8 \\ 4,6\end{array}$

### 4.6 More Trinomial Factoring

Recall: Factor $21-10 q+q^{2}$

$$
\begin{aligned}
& =q^{2}-10 q+21 \\
& =(q-3)(q-7)
\end{aligned}
$$



Working Forwards - notice the patterns:
Ex. 1 Expand
a) $(x+3 y)(x-5 y)$
b) $\left(x^{2}-3\right)\left(x^{2}-7\right)$
$=x^{2}-5 x y+3 x y-15 y^{2}$
$=x^{4}-7 x^{2}-3 x^{2}+21$
$=x^{2}-2 x y-15 y^{2}$
$=x^{4}-10 x^{2}+21$

Ex. 2 Factor

> a) $x^{4}+x^{2}-20$
> b) $x^{2}+8 x y+7 y^{2}$

$$
\text { c) } 12 m^{2}-10 m n-12 n^{2}
$$

How can we check to see if our

$$
=2\left(6 m^{2}-5 m n-6 n^{2}\right)
$$ factoring is correct?

$$
=2\left(6 m^{2}-9 m n+4 m n-6 n^{2}\right)
$$

$=2\left(6 m^{2}-9 m n+4 m n-6 n^{2}\right)$
$=2[3 m(2 m-3 n)+2 n(2 m-3 n)]$
$=2(2 m-3 n)(3 m+2 n) \frac{36}{1,36}$ m -36
2,18 A -5
$\frac{3,12}{4,9} \mathrm{n}, 6-9,4$

Quick Method

$=(x-2)(2 x+3) M-12$
NON-QUICK
$=2 x^{2}-4 x+3 x-6$
$=2 x(x-2)+3(x-2)$
$=(x-2)(2 x+3)$$\left\{\begin{array}{ll}\text { A }-1 & \text { 2. Write two fractions with } a \text { as the } \\ \text { numerator and the numbers as the } \\ \text { denominators. }\end{array}\right\} \begin{array}{ll}-\frac{2 x}{-4} & \frac{2 x}{3} \text { 3. Reduce the fractions, keeping the signs } \\ \text { where they are, and write as the }\end{array}$
$a x^{2}+b x+c$

1. Find two numbers that multiply to ac and add to $b$.

Ex. 2 Factor completely
a) $3 x^{2}-10 x+8$

$$
=(3 x-4)(x-2)
$$

$$
\frac{24}{1,24}
$$


b) $6 x^{2}-5 x-4$
$=(3 x-4)(2 x+1)$
M 24
A -10
$N \frac{3 x}{-4}, \frac{3 x}{-6}$
$\frac{3 x}{-4} \quad \frac{x}{-2}$


