



1. Expand and simplify  $-2(x - 3)(2x + 5)$

$$= -2(2x^2 - x - 15)$$

$$= -4x^2 + 2x + 30$$

2. Fully factor each of the following:

a)  $x^2 - 5x - 24$   
 $= (x - 8)(x + 3)$

b)  $4x^2 - 12x - 16$   
 $= 4(x^2 - 3x - 4)$   
 $= 4(x - 4)(x + 1)$

c)  $3x^2 - 12x - 16 + 4x$   
 $= 3x(x - 4) - 4(4 - x)$   
 $= 3x(x - 4) + 4(x - 4)$   
 $= (x - 4)(3x + 4)$

$$\begin{array}{r} 24 \\ \hline 1, 24 \\ 2, 12 \\ \hline 3, 8 \\ 4, 6 \end{array}$$

M - 24  
 A - 5  
 N - 8, 3

$$\begin{array}{r} -4 \\ \hline 1, 4 \\ \hline 2, 2 \end{array}$$

M - 4  
 A - 3  
 N - 4, 1

## 4.5 Factoring Complex Trinomials

$$x^2 - x - 20 \quad \text{simple trinomial} \quad a = 1$$

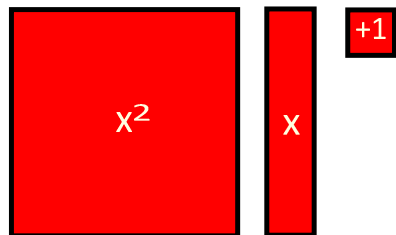
$$3x^2 - 5x - 2 \quad \text{complex trinomial} \quad a \neq 1$$



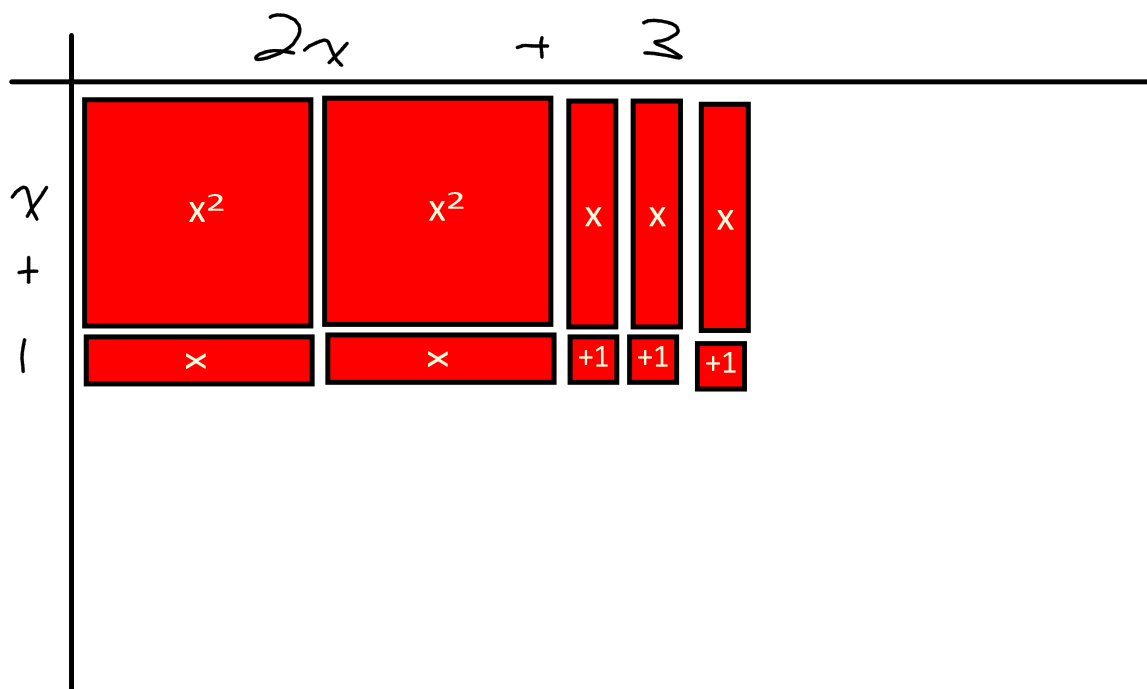
Always common factor first!

Ex. 1 Fully factor  $3x^2 + 3x - 6$

$$\begin{aligned}
 &= 3(x^2 + x - 2) & M & -2 \\
 &= 3(x-1)(x+2) & A & 1 \\
 & & N & -1, 2
 \end{aligned}$$



Factor  $2x^2 + 5x + 3$  using algebra tiles.



## Factoring by Decomposition

Expand  $(2x-1)(3x+5)$ 

$$\begin{aligned}(2x-1)(3x+5) &= 6x^2 + 10x - 3x - 5 \\ &= 6x^2 + 7x - 5\end{aligned}$$

Given  $6x^2 + 7x - 5$  you need a way of breaking up the middle term into  $10x$  and  $-3x$ .

$$\begin{array}{c} 6x^2 + 7x - 5 \\ 6x^2 + 10x - 3x - 5 \\ \swarrow \quad \searrow \\ -30 \end{array}$$

Use a M.A.N. table, but find the two numbers that:

Multiply to:  $A \times C$

Add to:  $B$

Once you have found the 2 numbers you can factor:

- use the numbers to break up the middle term
- factor by grouping

$$\begin{aligned}6x^2 + 7x - 5 &= 6x^2 + 10x - 3x - 5 \\ &= 2x(3x + 5) - 1(3x + 5) \\ &= (3x + 5)(2x - 1)\end{aligned}$$

$$\begin{array}{l} \text{M} \\ \text{A} \\ \text{N} \end{array} \quad \begin{array}{l} 6(-5) = -30 \\ 7 \\ 10, -3 \end{array}$$

Ex. 2 Factor by decomposition

a)  $12x^2 + 11x - 5$   
 $= 12x^2 - 4x + 15x - 5$   
 $= 4x(3x-1) + 5(3x-1)$   
 $= (3x-1)(4x+5)$

- M -60  
 A 11  
 N -4, 15
- 60  
 1, 60  
 2, 30  
 3, 20  
 4, 15  
 5, 12  
 6, 10

b)  $8x^2 - 2x - 3$   
 $= 8x^2 + 4x - 6x - 3$   
 $= 4x(2x+1) - 3(2x+1)$   
 $= (2x+1)(4x-3)$

- M -24  
 A -2  
 N 4, -6
- 24  
 1, 24  
 2, 12  
 3, 8  
 4, 6

c)  $10x^2 - 17x + 3$   
 M 30  
 A -17  
 N -2, -15

$= 10x^2 - 15x - 2x + 3$   
 $= 5x(2x-3) - (2x-3)$   
 $= (2x-3)(5x-1)$

- 30  
 1, 30  
 2, 15  
 3, 10  
 5, 6

d)  $12 + 18d + 8d^2$   
 $= 2(6 + 9d + 4d^2)$

- M 24  
 A 9  
 N

Not possible

- 24  
 1, 24  
 2, 12  
 3, 8  
 4, 6

# FBUHL

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**C1, 2cf, 4cdf, 5ace, 6acdf, 7c, 12, 13**

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